

SENSITIVITY ANALYSIS : A GRAPHICAL APPROACH TO ASSESS THE NECESSARY NUMBER OF SIMULATIONS IN A RANDOM SCANNING



S. Payraudeau (1)*, F. Cernesson (2), M.G. Tournoud (1),



(1) Laboratoire Hydrosociences, Université Montpellier 2 – CNRS – IRD (UMR5569), cc056 34095 Montpellier France,
 (2) Laboratoire Structures et Systèmes Spatiaux, CEMAGREF-ENGREF, 500 J.F. Breton 34093 Montpellier, France.
 *Contact : sylvain.payraudeau@msem.univ-montp2.fr



Introduction

A **sensitivity analysis** consists in scanning, in a random or systematic way, the entire range of each parameter of the model and in studying the variability of the output variables. A **random scanning** is usually more thrifty in simulations than a systematic scanning for a comparable description of the variability of the output variables (Gaume and al, 1998). The **choice of the number of simulations** is important because it conditions the duration and the exhaustiveness of the model sensitivity analysis (Saltelli, 2000). However, in random scanning, this number is **a priori unknown**.

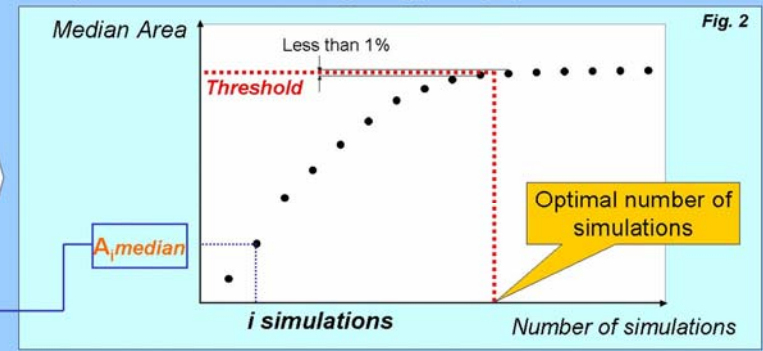
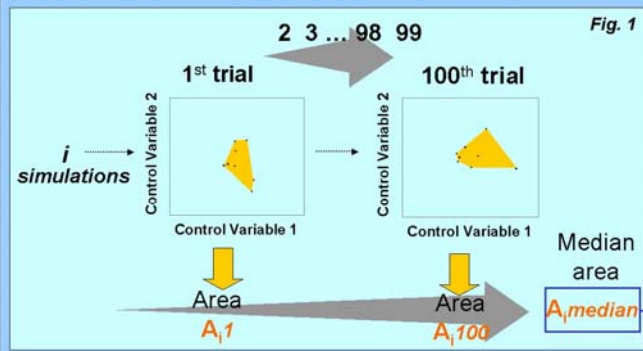
An **original method is proposed** allowing to determine the **optimal number of simulations**, to assess afterwards a full sensitivity analysis on two synthetic control variables.

Method

The method is based on the **analysis of the shape** obtained by plotting, in a two axis graph (control variable 1 versus control variable 2), the results **corresponding to different sets of parameters**. For each simulation, the set of parameters is randomly selected. The convex shape corresponding to the plotted points is extracted and the associated area is calculated with Arc-Info® tool. We study how **the area of the shape evolves** when the **number of simulations is increased**.

For a given number of simulations (i simulations in the Fig. 1), 100 trials are made. The median area corresponding to i simulations is calculated from the 100 area values.

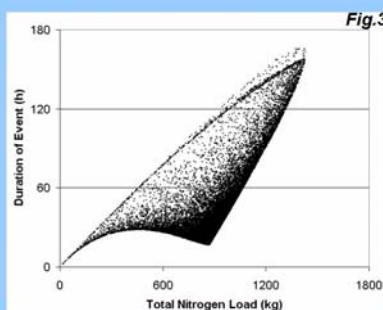
When the number of simulations is increased (from 2^2 to 2^{16}), the area increases until a threshold. The **optimal number of simulations** corresponds to the **threshold beginning** (cf. Fig. 2).



Application

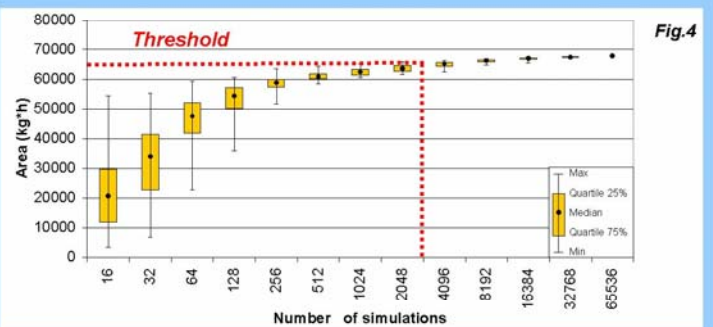
We applied this method on the model POL (Payraudeau and al, 2002). POL is a semi-distributed model developed to reproduce the daily nitrogen loads produced at the outlet of a catchment. The two synthetic control variables of model are the total nitrogen load produced during a flood event, and the duration of this event.

The figure 3 represents the shape of model output responses obtained with 65536 simulations.



How many simulations are necessary to correctly describe the model output variability ?

Results



A number of **4 000 simulations** is acceptable to obtained a steady output model area (cf. Fig. 4). For the same precision degree, a systematic scanning imposes more than one million simulations.

Conclusions

This method presents some advantages and limits :

- Advantages :**
- This statistical and geometrical method is **easily applicable** ;
 - The two synthetic control variables are **simultaneous analysed** ;
 - It can be applied in the case of models presenting a **great number of parameters**.

- Limits :**
- The **distribution of the plotted points** in the shape is not taking into account ;
 - This method is applicable for a model with **two synthetic control variables**.

This study has been used to realize a full sensitivity analysis of the POL model (Payraudeau, 2002).

References

- Gaume E., Villeneuve J.P. and Desbordes M., 1998. Uncertainty assessment and analysis of the calibrated parameter values of an urban storm water quality model. *Journal of Hydrology*, Vol 210, n°1-4, pp 38-50.
- Payraudeau S., 2002. Modélisation distribuée des flux d'azote sur des petits bassins versants méditerranéens, PhD, 424 p.
- Payraudeau S., Tournoud M.G. and Cernesson F., 2002. An adapted modelling approach for the nitrogen load management on a catchment scale. 14th International Conference on computational methods in water resources, Edited by S. M. Hassanizadeh and R.J. Scotting. June 23-27, Delft, in press.
- Saltelli A., 2000. What is sensitivity analysis ? In *Mathematical and statistical methods for sensitivity analysis*, Saltelli A., Chan K. and Scott M. Probability and Statistics Series, J Wiley & Sons. pp 1-22.